

Conservation of Momentum Problems

Answer each question in the space provided. Be sure to show all of your work and box your answer(s).

1. A 0.25 kg cue ball is traveling to the right at 9.2 m/s when it strikes the 0.12 kg 8-ball which is at rest. After the linear collision occurs, the cue ball continues to the right with a velocity of 7.3 m/s. What is the velocity of the 8-ball after the collision?

$v_1 = 9.2 \text{ m/s}$ $v_2 = 0 \text{ m/s}$
 $m_1 = 0.25 \text{ kg}$ $m_2 = 0.12 \text{ kg}$
 $v_1' = 7.3 \text{ m/s}$ $v_2' = ?$

$$\sum p_i = \sum p_f$$

$$m_1 v_1 = m_1 v_1' + m_2 v_2'$$

$$v_2' = \frac{m_1 v_1 - m_1 v_1'}{m_2}$$

$$v_2' = \frac{(0.25)(9.2) - (0.25)(7.3)}{0.12}$$

$v_2' = 3.96 \text{ m/s}$

2. A 3.5 kg toy truck is moving to the right at 1.7 m/s when a 0.5 kg piece of clay is thrown to the right at 6.5 m/s. If the clay sticks to the truck, what is the final velocity of the system after the collision?

$v_1 = 6.5 \text{ m/s}$ $v_2 = 1.7 \text{ m/s}$
 $m_1 = 0.5 \text{ kg}$ $m_2 = 3.5 \text{ kg}$
 $v' = ?$

$$\sum p_i = \sum p_f$$

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v'$$

$$v' = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$

$$v' = \frac{(0.5)(6.5) + (3.5)(1.7)}{(0.5 + 3.5)}$$

$v' = 2.3 \text{ m/s}$

3. A loaded 300 kg cannon at rest fires a 10 kg projectile at a velocity of 200 m/s to the right. What is the velocity of the cannon as it recoils backwards?

$v = 0$
 $m_1 = 300 \text{ kg}$ $m_2 = 10 \text{ kg}$
 $v_2' = 200 \text{ m/s}$
 $v_1' = ?$

$$\sum p_i = \sum p_f$$

$$0 = m_1 v_1' + m_2 v_2'$$

$$v_1' = \frac{-m_2 v_2'}{m_1}$$

$$v_1' = \frac{-(10)(200)}{300}$$

$v_1' = -6.67 \text{ m/s}$

4. Two identical gumballs, each with a mass of 0.045 kg, are rolling toward each other on a flat surface. The red gumball is moving to the right with a velocity of 1.3 m/s, and the blue gumball is moving to the left with a velocity of 0.75 m/s when they collide in an elastic collision. If, after the collision, the blue gumball is traveling to the right with a velocity of 2.3 m/s, what is the final velocity of the red gumball?

$v_1 = 1.3 \text{ m/s}$ $v_2 = -0.75 \text{ m/s}$
 $m_1 = 0.045 \text{ kg}$ $m_2 = 0.045 \text{ kg}$
 $v_2' = 2.3 \text{ m/s}$
 $v_1' = ?$

$$\sum p_i = \sum p_f$$

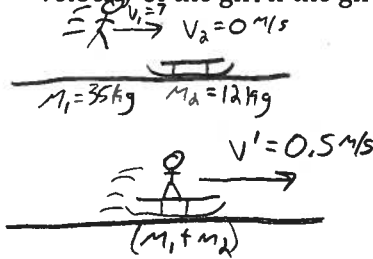
$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

$$v_1' = \frac{m_1 v_1 + m_2 v_2 - m_2 v_2'}{m_1}$$

$$v_1' = \frac{(0.045)(1.3) + (0.045)(-0.75) - (0.045)(2.3)}{(0.045)}$$

$v_1' = -1.75 \text{ m/s}$

5. A 35 kg girl jumps on to a 12 kg sled that is resting on some frictionless ice. What was the initial velocity of the girl if the girl and sled move forward with a velocity of 0.5 m/s?



$$\Sigma p_i = \Sigma p_f$$

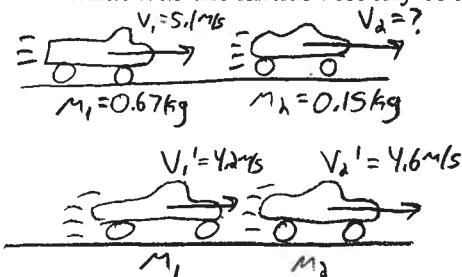
$$m_1 v_i = (m_1 + m_2) v'$$

$$v_i = \frac{(m_1 + m_2) v'}{m_1}$$

$$v_i = \frac{(35 + 12)(0.5)}{35}$$

$$v_i = 0.67 \text{ m/s}$$

6. A toy truck with a mass of 0.67 kg is moving to the right with a velocity of 5.1 m/s when it strikes a toy car that has a mass of 0.15 kg and is also moving to the right. If, after the collision, the velocity of the truck is 4.2 m/s to the right and the velocity of the car is 4.6 m/s to the right, what was the initial velocity of the car?



$$\Sigma p_i = \Sigma p_f$$

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

$$v_2 = \frac{m_1 v_1' + m_2 v_2' - m_1 v_1}{m_2}$$

$$v_2 = \frac{(0.67)(4.2) + (0.15)(4.6) - (0.67)(5.1)}{0.15}$$

$$v_2 = 0.58 \text{ m/s}$$

7. A 64 kg woman and her 32 kg son are standing together at rest on some frictionless ice. The woman pushes on the boy, sending him moving to the right with a velocity of 2.2 m/s. What is the velocity of the woman after the push?

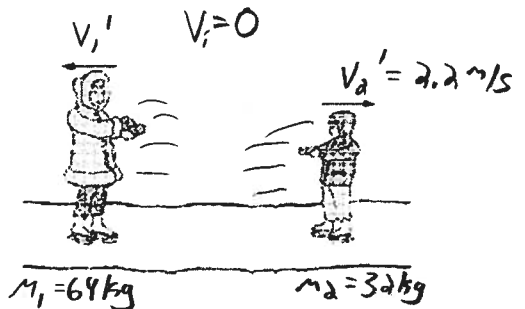
$$\Sigma p_i = \Sigma p_f$$

$$0 = m_1 v_1' + m_2 v_2'$$

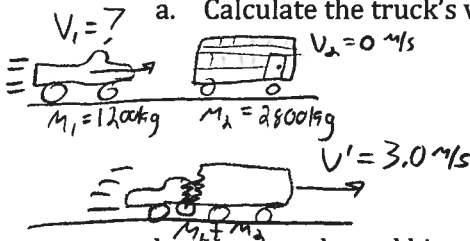
$$v_1' = \frac{-m_2 v_2'}{m_1}$$

$$v_1' = -\frac{(32)(2.2)}{64}$$

$$v_1' = -1.1 \text{ m/s}$$



8. The longest passenger buses in the world operate in Zaire. These buses have a mass of 2800 kg. Imagine a safety test involving one of these buses and a truck with a mass of 1200 kg. The truck with an unknown velocity travels to the right and hits a bus that is at rest so that the two vehicles move rightward together with a speed of 3.0 m/s.



a. Calculate the truck's velocity prior to the collision.

$$\Sigma p_i = \Sigma p_f$$

$$m_1 v_i = (m_1 + m_2) v'$$

$$v_i = \frac{(m_1 + m_2) v'}{m_1}$$

$$v_i = \frac{(1200 + 2800)(3)}{1200}$$

$$v_i = 10 \text{ m/s}$$

- b. How much total kinetic energy was lost in the collision?

$$KE_i = \frac{1}{2} m_1 v_i^2 = \frac{1}{2} (1200)(10)^2 = 60,000 \text{ J}$$

$$KE_f = \frac{1}{2} (m_1 + m_2) (v')^2 = \frac{1}{2} (1200 + 2800)(3)^2 = 18,000 \text{ J}$$

$$KE_{lost} = 60,000 - 18,000$$

$$KE_{lost} = 42,000 \text{ J}$$

9. Betty has a mass of 48 kg and is riding in a 9.5 kg wagon with a velocity of 0.75 m/s when she jumps out of the front of the wagon. The wagon recoils backwards with a velocity of 1.25 m/s. What is Betty's velocity after she jumps?

Diagram: A person and a wagon are shown moving to the right with velocity $V = 0.75 \text{ m/s}$. The total mass is $m_1 + m_2$. After separation, the wagon moves to the left with velocity $v_1' = -1.25 \text{ m/s}$ and the person moves to the right with velocity $v_2' = ?$. The wagon mass is $m_1 = 9.5 \text{ kg}$ and the person mass is $m_2 = 48 \text{ kg}$.

$$\sum p_i = \sum p_f$$

$$(m_1 + m_2)V = m_1 v_1' + m_2 v_2'$$

$$v_2' = \frac{(m_1 + m_2)V - m_1 v_1'}{m_2}$$

$$v_2' = \frac{(9.5 + 48)(0.75) - (9.5)(-1.25)}{48}$$

$$v_2' = 1.15 \text{ m/s}$$

10. Suppose a 0.045 kg golf ball is moving to the right at 75.8 m/s and strikes another ball that is at rest. After collision the golf ball rebounds backwards at 25.3 m/s and the other ball moves forward at 40.6 m/s.

a. What is the mass of second ball?

Diagram: A golf ball of mass $m_1 = 0.045 \text{ kg}$ moves to the right with velocity $v_1 = 75.8 \text{ m/s}$. A second ball of mass $m_2 = ?$ is at rest ($v_2 = 0$). After collision, the first ball moves to the left with velocity $v_1' = -25.3 \text{ m/s}$ and the second ball moves to the right with velocity $v_2' = 40.6 \text{ m/s}$.

$$\sum p_i = \sum p_f$$

$$m_1 v_1 = m_1 v_1' + m_2 v_2'$$

$$m_2 = \frac{m_1 v_1 - m_1 v_1'}{v_2'}$$

$$m_2 = \frac{(0.045)(75.8) - (0.045)(-25.3)}{40.6}$$

$$m_2 = 0.112 \text{ kg}$$

b. Is this an elastic or inelastic collision? Justify your answer.

$$\sum KE_i = \frac{1}{2} m_1 v_1^2 = \frac{1}{2} (0.045)(75.8)^2 = 129.3 \text{ J}$$

$$\sum KE_f = \frac{1}{2} m_1 (v_1')^2 + \frac{1}{2} m_2 (v_2')^2 = \frac{1}{2} (0.045)(-25.3)^2 + \frac{1}{2} (0.112)(40.6)^2 = 106.7 \text{ J}$$

It is inelastic, because KE is lost in the collision.

11. Two trains, each with a mass of 15,000 kg are moving toward each other. One train is moving with a velocity of 3.9 m/s to the left while the other is moving with a velocity of 0.5 m/s to the right. The two trains collide and lock together.

a. What is the velocity of the two trains after the collision?

Diagram: Two trains of mass $m_1 = 15000 \text{ kg}$ and $m_2 = 15000 \text{ kg}$ are moving toward each other. The first train moves to the right with velocity $v_1 = 3.9 \text{ m/s}$ and the second train moves to the left with velocity $v_2 = -0.5 \text{ m/s}$. After collision, they lock together and move with velocity $v' = ?$.

$$\sum p_i = \sum p_f$$

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v'$$

$$v' = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$

$$v' = \frac{(15000)(3.9) + (15000)(-0.5)}{30000}$$

$$v' = 1.7 \text{ m/s}$$

b. The two trains now collide and connect with a third train of mass 10,000 kg that is at rest. What is the velocity of the system of trains after this collision?

Diagram: The two trains from part (a) are now moving to the right with velocity $V = 1.7 \text{ m/s}$ and have a combined mass $m_1 + m_2$. A third train of mass $m_3 = 10,000 \text{ kg}$ is at rest ($v_3 = 0$). After collision, the three trains lock together and move with velocity $v' = ?$.

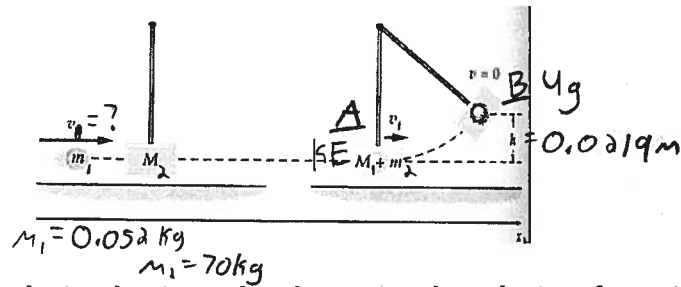
$$\sum p_i = \sum p_f$$

$$(m_1 + m_2)V = (m_1 + m_2 + m_3)v'$$

$$v' = \frac{(m_1 + m_2)V}{(m_1 + m_2 + m_3)}$$

$$v' = \frac{(30,000)(1.7)}{40,000}$$

$$v' = 1.275 \text{ m/s}$$



12. A ballistic pendulum is a device that is used to determine the velocity of a projectile, such as a bullet fired from a gun. The projectile is fired into a block of ballistic material that is suspended from a string, as in the diagram. The projectile comes to rest in the block and the system swings upward to a certain maximum height, which can be measured. Suppose a bullet with a mass of 52 grams is fired into a block that has a mass of 70 kg. The bullet comes to rest inside the block and the system swings upward to a maximum height of ~~0.0219~~ centimeters above where it started. What was the initial velocity of the bullet? 2.19cm
 (hint: you will need to apply the law of conservation of energy as well as the law of conservation of momentum to solve this problem)

$$\sum p_i = \sum p_f$$

$$m_1 v_1 = (m_1 + m_2) v'$$

$$v_1 = \frac{(m_1 + m_2) v'}{m_1}$$

$$v_1 = \frac{(0.052 + 70)(0.655)}{0.052}$$

$$v_1 = 883 \text{ m/s}$$

$$\sum E_A = \sum E_B$$

$$KE_A = U_{gB}$$

$$\frac{1}{2} (m_1 + m_2) (v')^2 = (m_1 + m_2) g h_B$$

$$v' = \sqrt{2 g h_B}$$

$$v' = \sqrt{2(9.8)(0.0219)}$$

$$v' = 0.655 \text{ m/s}$$